

Biological Process Engineering

An Analogical Approach to Fluid Flow, Heat Transfer, and Mass Transfer Applied to Biological Systems

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This book is dedicated to
all the little children in my life
who made me smile
even on the grayest of days.

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